

Does the ‘Higgs’ have Spin Zero?

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Abstract

The Higgs boson is predicted to have spin zero. The ATLAS and CMS experiments have recently reported of an excess of events with mass ~ 125 GeV that has some of the characteristics expected for a Higgs boson. We address the questions whether there is already any evidence that this excess has spin zero, and how this possibility could be confirmed in the near future. The excess observed in the $\gamma\gamma$ final state could not have spin one, leaving zero and two as open possibilities. We calculate the angular distribution of $\gamma\gamma$ pairs from the decays of a spin-two boson produced in gluon-gluon collisions, showing that is unique and distinct from the spin-zero case. We also calculate the distributions for lepton pairs that would be produced in the WW^* decays of a spin-two boson, which are very different from those in Higgs decays, and argue that the kinematics of the event selection used to produce the excess observed in the WW^* final state disfavors spin two.

PACS numbers: 14.70.Kv Gravitons, 14.80.Bn Standard-model Higgs bosons, 13.85.Qk Inclusive production with identified leptons, photons, or other nonhadronic particles, 13.88.+e Polarization in interactions and scattering

1 Introduction

The Higgs boson is predicted to have spin zero. Since all known elementary particles have non-zero spin, this is a crucial property to be checked by experiment before one could claim that the quest for this ‘Holy Grail’ of particle physics has been concluded successfully. Reflecting the importance of this issue, there have been many studies of the potential of the LHC experiments for measuring the spin of any candidate for the Higgs boson [1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13], e.g., by using four-lepton final states to look at spin correlations in ZZ or ZZ^* decays [2, 4, 7, 9, 10, 11, 12, 13].

The ATLAS [14] and CMS [15] collaborations have recently reported evidence for excesses in $\gamma\gamma$ and ZZ^* that are consistent with expectations for a Standard Model Higgs boson, an interpretation supported by broader enhancements of less significance in WW^* , $\tau\tau$ and $\bar{b}b$ final states. The statistics in ZZ^* decays are as yet insufficient for an attempt to constrain the ‘Higgs’ spin, so in this paper we consider other ways to obtain an indication what it may be.

A spin-one state cannot decay into two identical vector bosons, so a peak observed in the $\gamma\gamma$ final state must have spin zero or two *. Fermion-antifermion final states could come from spin zero or spin one †, so observation of a ‘Higgs’ signal in either of the $\tau\tau$ or $\bar{b}b$ final states would favour the spin-zero hypothesis over the spin-two option. However, so far only CMS reports any enhancements in these channels, and they are each $\leq 1\sigma$ for a mass of 125 GeV [15], so not conclusive at the present time. Accordingly, we consider here the $\gamma\gamma$ and $WW^* \rightarrow \ell^+\ell^-\nu\bar{\nu}$ final states, which have been observed with greater significance by both ATLAS and CMS.

Under the assumption that P-wave fermion-antifermion collisions can be neglected, a spin-two particle could be produced either by gluon-gluon collisions or by vector-boson fusion. We consider here the production of a hypothetical spin-two particle X_2 via gluon-gluon fusion, which is the dominant production mechanism for producing a Higgs boson weighing ~ 125 GeV. For definiteness, we assume that the X_2 couplings are of the same form as a massive Kaluza-Klein graviton [16, 17, 18], though without committing ourselves to such an extra-dimensional framework.

We calculate first the angular distribution for $gg \rightarrow X_2 \rightarrow \gamma\gamma$, showing that the final-state angular distribution in the X_2 centre of mass system is completely determined. It is suppressed at large angles relative to the beams, and hence is in principle distinct from the isotropic distribution predicted for spin-zero Higgs decay.

We then turn to the $X_2 \rightarrow WW^* \rightarrow \ell^+\ell^-\nu\bar{\nu}$ final state, again assuming production by gluon-gluon fusion and the same couplings as in massive graviton models [16, 17, 18]. We note that the ATLAS and CMS searches for $WW^* \rightarrow \ell^+\ell^-\nu\bar{\nu}$ final states [14, 15] already incorporate a hypothesis about the spin of the ‘Higgs’ candidate. They make use of the observation in [19] that a spin-zero particle decaying into WW

*In principle, one could consider also higher even spins, but these would entail production and decay mechanisms involving orbital angular momentum factors that we ignore here.

†Again neglecting orbital angular momentum.

(or WW^*) would yield final states in which the W^+ and W^- would have opposite polarizations. Since the W^- decays exclusively into *left*-handed leptons, whereas the W^+ decays exclusively into *right*-handed leptons, the *anticorrelation* between the W^\pm polarizations expected in spin-zero Higgs decay would be transferred into a *correlation* between the momenta of the charged leptons in their decays. This correlation would manifest itself in the distributions of relative ℓ^\pm polar angles and a preference for a small azimuthal angle between the $\ell^+\ell^-$ pair, $\phi_{\ell^+\ell^-}$, with a relatively small invariant mass, $m_{\ell^+\ell^-}$. Both ATLAS and CMS select events with cuts based on these observations [14, 15].

We study the types of $\ell^+\ell^-$ correlations to be expected in the $WW^* \rightarrow \ell^+\ell^-\nu\bar{\nu}$ decays of a spin-two state. We find that their momenta tend to be *anticorrelated*, with distinctive features in both polar and azimuthal angle distributions, and hence quite distinct from those expected for the decays of a spin-zero state. Hence, the observation of Higgs-like $\ell^+\ell^-$ correlations in WW^* final states may already be *prima facie* evidence that ATLAS and CMS may be observing a spin-zero state. This possibility should be pursued with experimental simulations of spin-two $WW^* \rightarrow \ell^+\ell^-\nu\bar{\nu}$ decays using the results presented here, which would indicate how much data would be needed to confirm the result with a significant degree of confidence.

2 Preliminaries

2.1 Production Kinematics

Ideally, one would prefer to perform such a ‘Higgs’ spin analysis in the most model-independent way possible. However, the density matrix of a massive spin-two particle has many parameters, and the available statistics limit the complexity of the hypotheses one can test currently, so we are led to make motivated simplifying assumptions about the possible production mechanism of a massive spin-two state. Bosons are generally produced in pp collisions by $\bar{q}q$, gg or WW/ZZ collisions. However, neglecting orbital angular momentum, $\bar{q}q$ collisions can produce only spin-zero or -one states, so we are left with gg and WW/ZZ collisions. Since gg collisions are much more copious and simpler to analyze, we focus on them.

Neglecting initial-state transverse momentum and radiation, we may regard the gluons as massless spin-one particles whose momenta are aligned with the collision axis. As such, if one quantizes angular momentum along this axis, they are equally likely to be in the helicity states $|1, \pm 1\rangle$. We assume that there is no coherence between the final states in which different gluon helicity states collide. Therefore the initial-state combinations $|1, +1\rangle|1, +1\rangle$, $|1, +1\rangle|1, -1\rangle$, $|1, -1\rangle|1, +1\rangle$ and $|1, -1\rangle|1, -1\rangle$ are equally likely. Accordingly, the gg initial states are a combination of the $|2, +2\rangle$, $|2, 0\rangle$ and $|2, 0\rangle$ polarization states, described by a spin-two density matrix ρ_2 that has only

diagonal entries with relative weights

$$\rho_i = \frac{3}{7}(|22\rangle\langle 22| + \frac{1}{3}|20\rangle\langle 20| + |2-2\rangle\langle 2-2|) , \quad (1)$$

where the relative normalization of the $J_z = 0$ component is determined by the Clebsch-Gordan coefficients $\langle 2, 0 || 1, \pm 1 \rangle |1, \mp 1\rangle = 1/\sqrt{6}$.

We explore in the following sections the consequences of this observation for the possible decays of a hypothetical spin-two particle X_2 into $\gamma\gamma$ and W^+W^- final states at the LHC.

2.2 Polarization States

Before discussing further the kinematics and dynamics of X_2 production and decay, we briefly review and establish our notation for the polarization states of the spin-one and -two particles appearing in our analysis.

A massive spin-one particle with momentum $p^\mu = (p^0, p^1, p^2, p^3) = (E, 0, 0, p)$ has three independent polarization states given by

$$\epsilon^{+\mu} = (0, -\frac{1}{\sqrt{2}}, -\frac{i}{\sqrt{2}}, 0) , \quad (2)$$

$$\epsilon^{-\mu} = (0, +\frac{1}{\sqrt{2}}, -\frac{i}{\sqrt{2}}, 0) , \quad (3)$$

$$\epsilon^{0\mu} = (\frac{p}{m}, 0, 0, \frac{E}{m}) . \quad (4)$$

If we work in the Lorentz frame where the vector particle is at rest, so that $p^\mu = (p^0, p^1, p^2, p^3) = (m, 0, 0, 0)$, the three polarization vectors are given by (2), (3), and for (4)

$$\epsilon^{0\mu} = (0, 0, 0, 1) . \quad (5)$$

The polarization vectors $\epsilon^{+\mu}$, $\epsilon^{-\mu}$ and $\epsilon^{0\mu}$ correspond to the quantum states $|1, +1\rangle$, $|1, -1\rangle$ and $|1, 0\rangle$, respectively, with the z -axis as the quantization axis.

We now consider the spin states of a spin-two particle X_2 with mass m , in its rest frame. The polarizations of X_2 can be represented by the following polarization tensors:

$$\begin{aligned} \epsilon^{s\mu\nu} &= (|2+2\rangle, |2,+1\rangle, |2,0\rangle, |2,-1\rangle, |2,-2\rangle) \\ &= (\epsilon^{+2\mu\nu}, \epsilon^{+1\mu\nu}, \epsilon^{0\mu\nu}, \epsilon^{-1\mu\nu}, \epsilon^{-2\mu\nu}) \\ &= (\epsilon^{+\mu}\epsilon^{+\nu}, \frac{1}{\sqrt{2}}(\epsilon^{+\mu}\epsilon^{0\nu} + \epsilon^{0\mu}\epsilon^{+\nu}), \\ &\quad \frac{1}{\sqrt{6}}(\epsilon^{+\mu}\epsilon^{-\nu} + \epsilon^{-\mu}\epsilon^{+\nu} + 2\epsilon^{0\mu}\epsilon^{0\nu}), \frac{1}{\sqrt{2}}(\epsilon^{-\mu}\epsilon^{0\nu} + \epsilon^{0\mu}\epsilon^{-\nu}), \epsilon^{-\mu}\epsilon^{-\nu}) , \end{aligned} \quad (6)$$

where $\epsilon^{+\mu}$, $\epsilon^{-\mu}$ are given in (2) and (3), and $\epsilon^{0\mu}$ is given in (5), since we work in the X_2 rest frame.

The polarization tensors given in (6) satisfy the following relations:

$$(\epsilon^s)_\mu{}^\mu = 0, \quad p_\mu \epsilon^{s\mu\nu} = 0, \quad \epsilon^{s\mu\nu} \epsilon_{\mu\nu}^{s'*} = \delta^{ss'}, \quad (7)$$

and

$$\sum_{s=-2}^{+2} \epsilon_{\mu\nu}^s \epsilon_{\alpha\beta}^{s*} = B_{\mu\nu\ \alpha\beta}, \quad (8)$$

where

$$\begin{aligned} B_{\mu\nu\ \alpha\beta} = & \left(\eta_{\mu\alpha} - \frac{p_\mu p_\alpha}{m^2} \right) \left(\eta_{\nu\beta} - \frac{p_\nu p_\beta}{m^2} \right) + \left(\eta_{\mu\beta} - \frac{p_\mu p_\beta}{m^2} \right) \left(\eta_{\nu\alpha} - \frac{p_\nu p_\alpha}{m^2} \right) \\ & - \frac{2}{3} \left(\eta_{\mu\nu} - \frac{p_\mu p_\nu}{m^2} \right) \left(\eta_{\alpha\beta} - \frac{p_\alpha p_\beta}{m^2} \right). \end{aligned} \quad (9)$$

We further note that the propagator of the spin-two massive X_2 particle is given by [16, 17, 18]

$$i\Delta_{\mu\nu\ \alpha\beta} = \frac{i B_{\mu\nu\ \alpha\beta}}{p^2 - m^2 + i\varepsilon}. \quad (10)$$

3 The Process $gg \rightarrow X_2 \rightarrow \gamma\gamma$

3.1 Preliminaries

The three-point vertex for $X_2\gamma\gamma$ or gg is illustrated in Fig. 1(a), the process $gg \rightarrow X_2 \rightarrow \gamma\gamma$ is illustrated in Fig. 1(b), and our notation for the kinematics is illustrated in Fig. 1(c). For definiteness, we use the following Feynman rule for the $X_2\gamma\gamma$ vertex, which was derived in [16, 17] for the coupling of a massive Kaluza-Klein graviton:

$$- \frac{i}{M} \left(W_{\mu\nu\ \alpha\beta}^{(\gamma)} + W_{\nu\mu\ \alpha\beta}^{(\gamma)} \right), \quad (11)$$

where M is a normalization factor and

$$W_{\mu\nu\ \alpha\beta}^{(\gamma)} = \frac{1}{2} \eta_{\mu\nu} (-k_1 \cdot k_2 \eta_{\alpha\beta} + k_{1\beta} k_{2\alpha}) \quad (12)$$

$$+ k_1 \cdot k_2 \eta_{\mu\alpha} \eta_{\nu\beta} \quad (13)$$

$$- \eta_{\mu\alpha} k_{1\beta} k_{2\nu} - \eta_{\mu\beta} k_{1\nu} k_{2\alpha} \quad (14)$$

$$+ \eta_{\alpha\beta} k_{1\mu} k_{2\nu}. \quad (15)$$

The $X_2 gg$ vertex is identical, apart from a trivial color factor δ^{ab} .

We work in the X_2 rest frame, take the beam direction as the z -axis, and write the momenta of the initial-state gluons as

$$k_1^\mu = (k_1^0, k_1^1, k_1^2, k_1^3) = (k, 0, 0, k), \quad k_2^\mu = (k_1^0, k_1^1, k_1^2, k_1^3) = (k, 0, 0, -k). \quad (16)$$

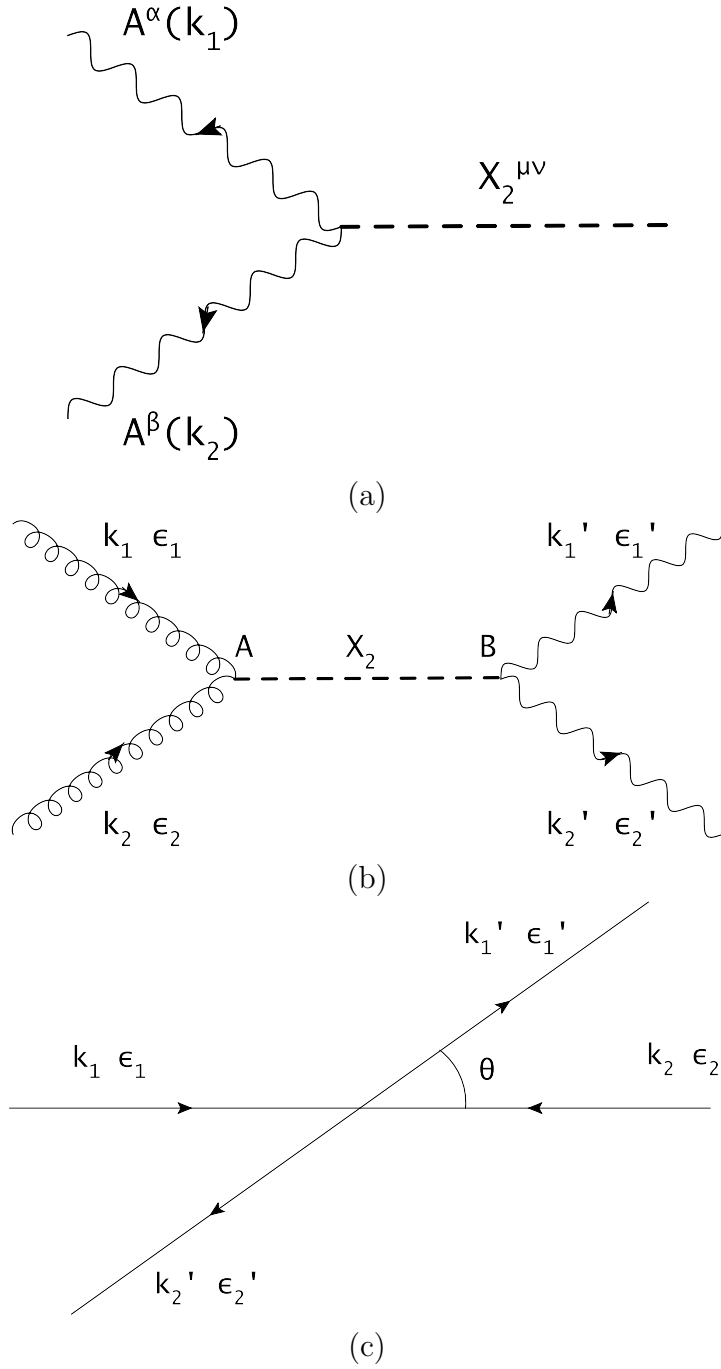


Figure 1: (a) The vertex coupling X_2 to two gauge fields, (b) Feynman diagram and (c) the kinematics for the process $gg \rightarrow X_2 \rightarrow \gamma\gamma$.

We recall that the polarization vectors of the massless initial-state gluons are given by (2) and (3).

We denote the unit spatial vectors in the coordinate system where (16), (2) and (3) apply for the initial-state gluons by \hat{x} , \hat{y} and \hat{z} . We denote the momenta of the final-state photons by k'_1 and k'_2 , and take the three-momentum vector of k'_1 to lie along the \hat{z}' direction, where \hat{x}' , \hat{y}' and \hat{z}' are given by

$$\hat{x}' = \cos \theta \hat{x} - \sin \theta \hat{z}, \quad \hat{z}' = \sin \theta \hat{x} + \cos \theta \hat{z}, \quad \hat{y}' = \hat{y}, \quad (17)$$

i.e., \hat{z}' is given by rotating \hat{z} toward \hat{x} by the angle θ , as shown in Fig. 1(c). The momenta k'_1 and k'_2 , as well as the polarization vectors of the final-state photons in the coordinate system \hat{x}' , \hat{y}' and \hat{z}' , are given by expressions identical to those given in (2), (3) and (16) for the initial-state gluons in the coordinate system \hat{x} , \hat{y} and \hat{z} . Then, in the coordinate system \hat{x} , \hat{y} and \hat{z} , we have

$$k'_1{}^\mu = k(1, \sin \theta, 0, \cos \theta), \quad k'_2{}^\mu = k(1, -\sin \theta, 0, -\cos \theta), \quad (18)$$

and

$$\epsilon'^{+\mu} = (0, -\frac{1}{\sqrt{2}} \cos \theta, -\frac{i}{\sqrt{2}}, \frac{1}{\sqrt{2}} \sin \theta), \quad \epsilon'^{-\mu} = (0, \frac{1}{\sqrt{2}} \cos \theta, -\frac{i}{\sqrt{2}}, -\frac{1}{\sqrt{2}} \sin \theta). \quad (19)$$

The three rotated polarizations of X_2 are represented by the two given in (19) and by

$$\epsilon'^{0\mu} = (0, \sin \theta, 0, \cos \theta). \quad (20)$$

The amplitude of the process $gg \rightarrow X_2 \rightarrow \gamma\gamma$ is proportional to

$$A(\epsilon'_1 \epsilon'_2; \epsilon_1 \epsilon_2) = \epsilon_1^{a*} \epsilon_2^{b*} W_{ab \rho\sigma} \left(\sum_{s=-2}^{+2} \epsilon^{s\rho\sigma} \epsilon^{s\mu\nu*} \right) W_{\mu\nu \alpha\beta} \epsilon_1^\alpha \epsilon_2^\beta, \quad (21)$$

where the vertex $W_{\mu\nu \alpha\beta}$ is given in (11).

3.2 Calculation of Differential Cross Section

We calculate the amplitude for $gg \rightarrow X_2 \rightarrow \gamma\gamma$ when the initial gluon polarization state is one of $\epsilon_1^+ \epsilon_2^+$, $\epsilon_1^- \epsilon_2^-$, $\epsilon_1^+ \epsilon_2^-$ and $\epsilon_1^- \epsilon_2^+$, and the final photon polarization state is one of $\epsilon_1'^+ \epsilon_2'^+$, $\epsilon_1'^- \epsilon_2'^-$, $\epsilon_1'^+ \epsilon_2'^-$ and $\epsilon_1'^- \epsilon_2'^+$, via the Feynman diagram drawn in Fig. 1(b).

Using the first equation in (7), we see that (12) does not contribute to the amplitudes. Moreover, we see from (2), (3) and (16), that $k_1 \cdot \epsilon_2 = k_2 \cdot \epsilon_1 = 0$ and hence (14) also does not contribute to the amplitudes. Therefore, only the terms (13) and (15) in $W_{\mu\nu \alpha\beta}^{(\gamma)}$ may contribute to the amplitudes.

We find that the amplitude for $gg \rightarrow X_2 \rightarrow \gamma\gamma$ is non-zero only when *both* of the following two conditions are satisfied: (1) the initial gluon polarization state is one of

$\epsilon_1^+ \epsilon_2^+$ and $\epsilon_1^- \epsilon_2^-$, and (2) the final photon polarization state is one of $\epsilon_1'^+ \epsilon_2'^+$ and $\epsilon_1'^- \epsilon_2'^-$. On the other hand, the amplitude is zero either when the initial gluon polarization state is one of $\epsilon_1^+ \epsilon_2^-$ and $\epsilon_1^- \epsilon_2^+$, or when the final photon polarization state is one of $\epsilon_1'^+ \epsilon_2'^-$ and $\epsilon_1'^- \epsilon_2'^+$.

We consider the vertex $gg \rightarrow X_2$ in the process $gg \rightarrow X_2 \rightarrow \gamma\gamma$, which corresponds to the vertex A in Fig. 1(b). When the expression (15), i.e., $\eta_{\alpha\beta} k_{1\mu} k_{2\nu}$, is attached at this vertex, this vertex is non-zero only when the initial gluon polarization state is $\epsilon_1^+ \epsilon_2^-$ or $\epsilon_1^- \epsilon_2^+$, since $\eta_{\alpha\beta} \epsilon_1^{+\alpha} \epsilon_2^{-\beta} = \eta_{\alpha\beta} \epsilon_1^{-\alpha} \epsilon_2^{+\beta} = 1$ and $\eta_{\alpha\beta} \epsilon_1^{+\alpha} \epsilon_2^{+\beta} = \eta_{\alpha\beta} \epsilon_1^{-\alpha} \epsilon_2^{-\beta} = 0$. Then, using $\epsilon^{0\mu\nu*} k_{1\mu} k_{2\nu} = \frac{2}{\sqrt{6}} (\epsilon^{0*} \cdot k_1) (\epsilon^{0*} \cdot k_2) = \frac{2}{\sqrt{6}} (-k)(+k) = -\frac{2}{\sqrt{6}} k^2$ and $\epsilon^{(s \neq 0)\mu\nu*} k_{1\mu} k_{2\nu} = 0$, the amplitude (21) for this vertex becomes

$$\begin{aligned} & \epsilon_1'^{a*} \epsilon_2'^{b*} W_{ab \rho\sigma} \left(\sum_{s=-2}^{+2} \epsilon^{s\rho\sigma} \epsilon^{s\mu\nu*} \right) (\eta_{\alpha\beta} k_{1\mu} k_{2\nu}) \epsilon_1^{+\alpha} \epsilon_2^{-\beta} \\ &= \epsilon_1'^{a*} \epsilon_2'^{b*} W_{ab \rho\sigma} \left(\sum_{s=-2}^{+2} \epsilon^{s\rho\sigma} \epsilon^{s\mu\nu*} \right) (\eta_{\alpha\beta} k_{1\mu} k_{2\nu}) \epsilon_1^{-\alpha} \epsilon_2^{+\beta} \\ &= \epsilon_1'^{a*} \epsilon_2'^{b*} W_{ab \rho\sigma} \epsilon^{0\rho\sigma} \left(-\frac{2}{\sqrt{6}} k^2 \right), \end{aligned} \quad (22)$$

and

$$\begin{aligned} & \epsilon_1'^{a*} \epsilon_2'^{b*} W_{ab \rho\sigma} \left(\sum_{s=-2}^{+2} \epsilon^{s\rho\sigma} \epsilon^{s\mu\nu*} \right) (\eta_{\alpha\beta} k_{1\mu} k_{2\nu}) \epsilon_1^{+\alpha} \epsilon_2^{+\beta} \\ &= \epsilon_1'^{a*} \epsilon_2'^{b*} W_{ab \rho\sigma} \left(\sum_{s=-2}^{+2} \epsilon^{s\rho\sigma} \epsilon^{s\mu\nu*} \right) (\eta_{\alpha\beta} k_{1\mu} k_{2\nu}) \epsilon_1^{-\alpha} \epsilon_2^{-\beta} \\ &= 0. \end{aligned} \quad (23)$$

When the expression (13), i.e., $k_1 \cdot k_2 \eta_{\mu\alpha} \eta_{\nu\beta}$, is attached at this vertex, using $\epsilon^{+*} \cdot \epsilon_1^+ = \epsilon^{-*} \cdot \epsilon_1^- = \epsilon^{+*} \cdot \epsilon_2^+ = \epsilon^{-*} \cdot \epsilon_2^- = -1$ and $k_1 \cdot k_2 = 2k^2$, we find

$$\begin{aligned} & \epsilon_1'^{a*} \epsilon_2'^{b*} W_{ab \rho\sigma} \left(\sum_{s=-2}^{+2} \epsilon^{s\rho\sigma} \epsilon^{s\mu\nu*} \right) (k_1 \cdot k_2 \eta_{\mu\alpha} \eta_{\nu\beta}) \epsilon_1^{+\alpha} \epsilon_2^{-\beta} \\ &= \epsilon_1'^{a*} \epsilon_2'^{b*} W_{ab \rho\sigma} \left(\sum_{s=-2}^{+2} \epsilon^{s\rho\sigma} \epsilon^{s\mu\nu*} \right) (k_1 \cdot k_2 \eta_{\mu\alpha} \eta_{\nu\beta}) \epsilon_1^{-\alpha} \epsilon_2^{+\beta} \\ &= \epsilon_1'^{a*} \epsilon_2'^{b*} W_{ab \rho\sigma} \epsilon^{0\rho\sigma} \left(+\frac{1}{\sqrt{6}} 2k^2 \right), \end{aligned} \quad (24)$$

and

$$\begin{aligned} & \epsilon_1'^{a*} \epsilon_2'^{b*} W_{ab \rho\sigma} \left(\sum_{s=-2}^{+2} \epsilon^{s\rho\sigma} \epsilon^{s\mu\nu*} \right) (k_1 \cdot k_2 \eta_{\mu\alpha} \eta_{\nu\beta}) \epsilon_1^{+\alpha} \epsilon_2^{+\beta} = \epsilon_1'^{a*} \epsilon_2'^{b*} W_{ab \rho\sigma} \epsilon^{+2\rho\sigma} (2k^2) \\ & \epsilon_1'^{a*} \epsilon_2'^{b*} W_{ab \rho\sigma} \left(\sum_{s=-2}^{+2} \epsilon^{s\rho\sigma} \epsilon^{s\mu\nu*} \right) (k_1 \cdot k_2 \eta_{\mu\alpha} \eta_{\nu\beta}) \epsilon_1^{-\alpha} \epsilon_2^{-\beta} = \epsilon_1'^{a*} \epsilon_2'^{b*} W_{ab \rho\sigma} \epsilon^{-2\rho\sigma} (2k^2). \end{aligned} \quad (25)$$

Combining (22) to (25), we have

$$\begin{aligned}
& \epsilon_1'^a * \epsilon_2'^b * W_{ab \rho\sigma} \left(\sum_{s=-2}^{+2} \epsilon^{s\rho\sigma} \epsilon^{s\mu\nu *} \right) \left(k_1 \cdot k_2 \eta_{\mu\alpha} \eta_{\nu\beta} + \eta_{\alpha\beta} k_{1\mu} k_{2\nu} \right) \epsilon_1^{+\alpha} \epsilon_2^{-\beta} \\
&= \epsilon_1'^a * \epsilon_2'^b * W_{ab \rho\sigma} \left(\sum_{s=-2}^{+2} \epsilon^{s\rho\sigma} \epsilon^{s\mu\nu *} \right) \left(k_1 \cdot k_2 \eta_{\mu\alpha} \eta_{\nu\beta} + \eta_{\alpha\beta} k_{1\mu} k_{2\nu} \right) \epsilon_1^{-\alpha} \epsilon_2^{+\beta} \\
&= 0,
\end{aligned} \tag{26}$$

and

$$\begin{aligned}
& \epsilon_1'^a * \epsilon_2'^b * W_{ab \rho\sigma} \left(\sum_{s=-2}^{+2} \epsilon^{s\rho\sigma} \epsilon^{s\mu\nu *} \right) \left(k_1 \cdot k_2 \eta_{\mu\alpha} \eta_{\nu\beta} + \eta_{\alpha\beta} k_{1\mu} k_{2\nu} \right) \epsilon_1^{+\alpha} \epsilon_2^{+\beta} \\
&= \epsilon_1'^a * \epsilon_2'^b * W_{ab \rho\sigma} \epsilon^{+2\rho\sigma} (2k^2), \\
& \epsilon_1'^a * \epsilon_2'^b * W_{ab \rho\sigma} \left(\sum_{s=-2}^{+2} \epsilon^{s\rho\sigma} \epsilon^{s\mu\nu *} \right) \left(k_1 \cdot k_2 \eta_{\mu\alpha} \eta_{\nu\beta} + \eta_{\alpha\beta} k_{1\mu} k_{2\nu} \right) \epsilon_1^{-\alpha} \epsilon_2^{-\beta} \\
&= \epsilon_1'^a * \epsilon_2'^b * W_{ab \rho\sigma} \epsilon^{-2\rho\sigma} (2k^2).
\end{aligned} \tag{27}$$

Equivalent results are obtained when the roles of the initial gluon polarization states and the final photon polarization states are exchanged in (26) and (27).

This analysis justifies the statement made at the beginning of this subsection, namely that the amplitude for $gg \rightarrow X_2 \rightarrow \gamma\gamma$ is non-zero only when *both* of the following two conditions are satisfied: (1) the initial gluon polarization state is one of $\epsilon_1^+ \epsilon_2^+$ and $\epsilon_1^- \epsilon_2^-$, *and* (2) the final photon polarization state is one of $\epsilon_1'^+ \epsilon_2'^+$ and $\epsilon_1'^- \epsilon_2'^-$. That is, the amplitude is zero *either* when the initial gluon polarization state is one of $\epsilon_1^+ \epsilon_2^-$ and $\epsilon_1^- \epsilon_2^+$, *or* when the final photon polarization state is one of $\epsilon_1'^+ \epsilon_2'^-$ and $\epsilon_1'^- \epsilon_2'^+$.

We also see in (27) that in the non-zero amplitude found when both (13) and (15) are attached at both vertices in the Feynman diagram is the same as that obtained when only (13) is attached at both vertices in the Feynman diagram.

When the sum of (13) and (15), i.e., $(k_1 \cdot k_2 \eta_{\mu\alpha} \eta_{\nu\beta} + \eta_{\alpha\beta} k_{1\mu} k_{2\nu})$, is attached at both vertices in the Feynman diagram for $gg \rightarrow X_2 \rightarrow \gamma\gamma$ shown in Fig. 1(b), using (2), (3), (6) and (19) in (27), we find that the amplitudes (21) are given by $(4k^2/M)^2$ times the following angular expressions:

$$A(+'+';++) = A(-'-';--) = \frac{1}{4}(1 + \cos\theta)^2 \tag{28}$$

$$A(-'-';++) = A(+'+';--) = \frac{1}{4}(1 - \cos\theta)^2 \tag{29}$$

$$A(+'-';++) = A(-'+';++) = A(+'-';--) = A(-'+';--) = 0 \tag{30}$$

$$A(+'+';+-) = A(-'-';+-) = A(+'+';-+) = A(-'-';-+) = 0 \tag{31}$$

$$A(+'-';+-) = A(-'+';+-) = A(+'-';-+) = A(-'+';-+) = 0. \tag{32}$$

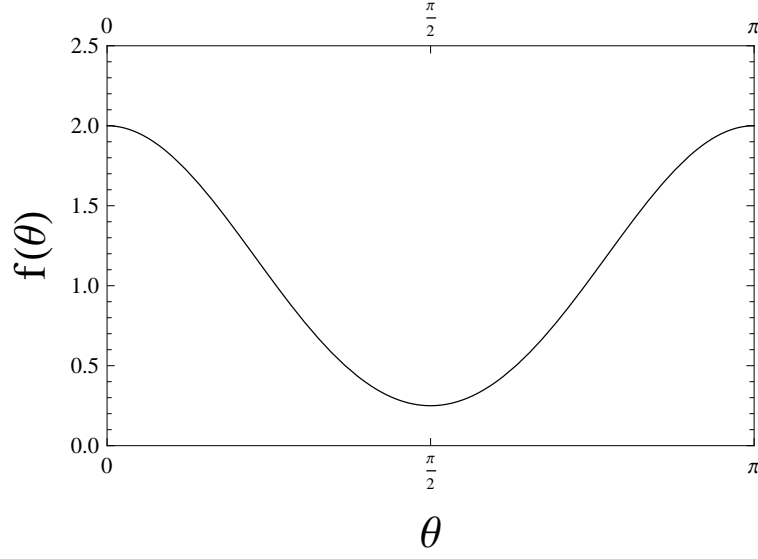


Figure 2: The $\gamma\gamma$ angular distribution of $d\sigma/d\Omega$ given in (33).

The contributions of the two possible final polarization states $\epsilon_1^+\epsilon_2^+$ and $\epsilon_1^-\epsilon_2^-$ to the total $\gamma\gamma$ cross section $d\sigma/d\Omega$ are identical, and we have

$$\frac{d\sigma}{d\Omega} \propto \frac{1}{4} + \frac{3}{2}\cos^2\theta + \frac{1}{4}\cos^4\theta, \quad (33)$$

which is plotted in Fig. 2.

We see in Fig. 2 that the total $\gamma\gamma$ angular distribution in the X_2 centre-of-mass frame differs substantially from the isotropic angular distribution expected for the decay of a spin-zero particle such as the Higgs boson. In particular, the $\gamma\gamma$ final state is suppressed at large angles θ relative to the beams. This suggests that a careful study of the $\gamma\gamma$ angular distribution might offer some discrimination between the spin-two and spin-zero hypotheses. However, any conclusion on this possibility would require a realistic simulation of the $\gamma\gamma$ signal in an LHC detector.

4 The Process $gg \rightarrow X_2 \rightarrow W^-W^+ \rightarrow \ell^-\ell^+\bar{\nu}\nu$

4.1 Lepton Angular Distributions in W Decays

4.1.1 $W^- \rightarrow \ell^-\bar{\nu}$

As preparation for this Section, we first consider the decay $W^- \rightarrow \ell^-\bar{\nu}$. We consider a W^- at rest and denote the momenta of the final-state particles by

$$p_{\ell^-}^\mu = (p, p \sin \theta_1 \cos \phi_1, p \sin \theta_1 \sin \phi_1, p \cos \theta_1), \quad (34)$$

$$p_{\bar{\nu}}^\mu = (p, -p \sin \theta_1 \cos \phi_1, -p \sin \theta_1 \sin \phi_1, -p \cos \theta_1), \quad (35)$$

where $p = |\vec{p}|$ and the ℓ^- mass is ignored. The polarization vectors ϵ of W^- with the z -axis as the quantization axis are given by (2, 3) and $\epsilon^{0\mu} = (0, 0, 0, 1)$. The vertex for this decay is given by

$$-ig_W \cos \theta_W \bar{u}(p_{\ell^-}) \gamma^\mu \epsilon_\mu (1 - \gamma_5) v(p_{\bar{\nu}}) . \quad (36)$$

We calculate

$$\mathcal{M}_1 = \bar{u}(p_{\ell^-}) \gamma^\mu \epsilon_{1\mu} (1 - \gamma_5) v(p_{\bar{\nu}}) , \quad (37)$$

and obtain the following results for $\mathcal{M}_1/(2\sqrt{2}p)$:

$$\text{for } \epsilon_1^+ , \quad (1 - \cos \theta_1) e^{-i\phi_1} \quad (38)$$

$$\text{for } \epsilon_1^- , \quad (1 + \cos \theta_1) e^{+i\phi_1} \quad (39)$$

$$\text{for } \epsilon_1^0 , \quad -\sqrt{2} \sin \theta_1 . \quad (40)$$

The differential cross section $d\sigma/d\Omega$ is proportional to $|\mathcal{M}_1|^2$ and the functions $f(\theta) = |\mathcal{M}_1/(2\sqrt{2}p)|^2$ for the three polarization states are plotted in Fig. 3.

4.1.2 $W^+ \rightarrow \ell^+ \nu$

In the case of W^+ at rest, we denote the momenta of the final-state particles by

$$p_{\ell^+}^\mu = (p, p \sin \theta_2 \cos \phi_2, p \sin \theta_2 \sin \phi_2, p \cos \theta_2) , \quad (41)$$

$$p_\nu^\mu = (p, -p \sin \theta_2 \cos \phi_2, -p \sin \theta_2 \sin \phi_2, -p \cos \theta_2) , \quad (42)$$

where $p = |\vec{p}|$ and the ℓ^+ mass is ignored. The polarization vectors ϵ of W^+ with the z -axis as the quantization axis are given by (2, 3) and $\epsilon^{0\mu} = (0, 0, 0, 1)$. The vertex for this decay is given by

$$-ig_W \cos \theta_W \bar{u}(p_\nu) \gamma^\mu \epsilon_{2\mu} (1 - \gamma_5) v(p_{\ell^+}) . \quad (43)$$

We calculate

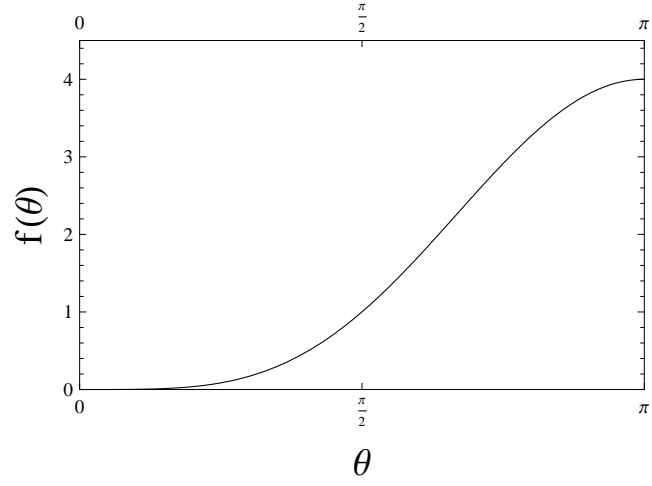
$$\mathcal{M}_2 = \bar{u}(p_\nu) \gamma^\mu \epsilon_{2\mu} (1 - \gamma_5) v(p_{\ell^+}) , \quad (44)$$

and obtain the following results for $\mathcal{M}_2/(2\sqrt{2}p)$:

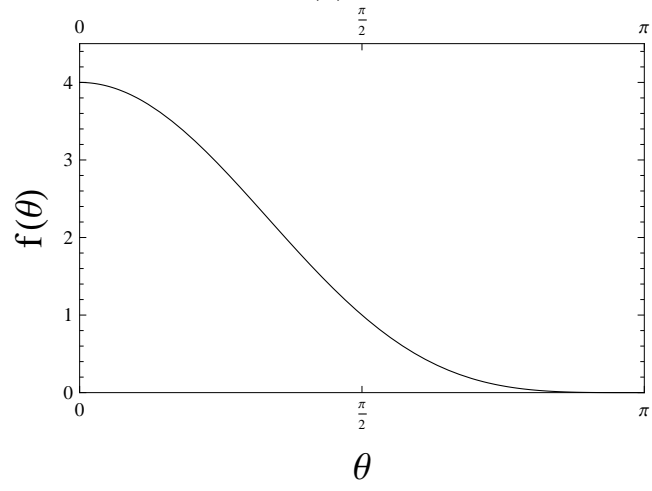
$$\text{for } \epsilon_2^+ , \quad -(1 + \cos \theta_2) e^{-i\phi_2} \quad (45)$$

$$\text{for } \epsilon_2^- , \quad -(1 - \cos \theta_2) e^{+i\phi_2} \quad (46)$$

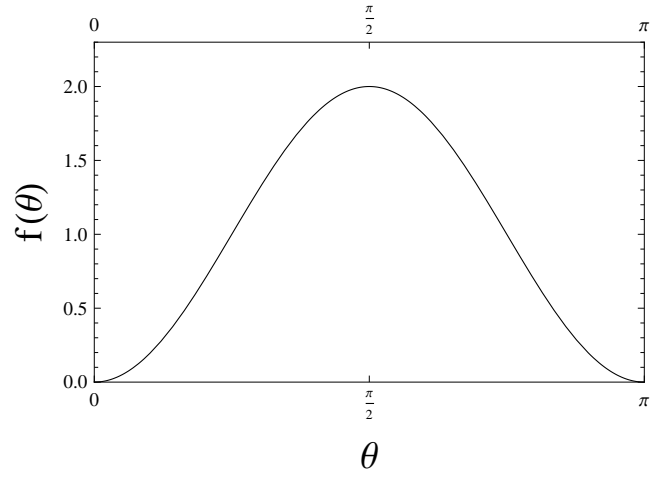
$$\text{for } \epsilon_2^0 , \quad -\sqrt{2} \sin \theta_2 . \quad (47)$$



(a)



(b)



(c)

Figure 3: The decay angular distribution functions $f(\theta)$ in $W^- \rightarrow \ell^- \bar{\nu}$ decays from the W^- polarization states given by (a) ϵ^+ , (b) ϵ^- , and (c) ϵ^0 .

4.2 Angular Distributions in $gg \rightarrow X_2(X_0) \rightarrow W^-W^+ \rightarrow \ell^-\ell^+\bar{\nu}\nu$

For simplicity, we assume that the W^- and W^+ are at rest, corresponding to the case that $m_X = 2m_W$. In practice, we are interested in the decay of the possible particle with mass ~ 125 GeV reported by ATLAS and CMS, which would decay into one on-shell W and one off-shell $W^* \rightarrow \ell\nu$. The structure of the $W\ell\nu$ decay matrix element would be dominated by the W^* pole, favouring $\ell\nu$ invariant masses close to $m_X - m_W$ and hence small momenta for the W and W^* in the centre-of-mass frame of the decaying X particle. The crude approximation of neglecting these momenta may serve to indicate whether in principle there could be significant differences between the decay angular distributions in X_2 and X_0 decay that could be investigated in more detailed simulations.

With this assumption, we denote the polarization vector and momentum of the W^- (W^+) by ϵ_1 and k_1 (ϵ_2 and k_2), respectively. The polarization vectors ϵ_1 and ϵ_2 with the z -axis as the quantization axis are given by given by (2, 3) and $\epsilon^{0\mu} = (0, 0, 0, 1)$ as before, and the momenta k_1 and k_2 are given by

$$k_1^\mu = k_2^\mu = (k_1^0, k_1^1, k_1^2, k_1^3) = (m_W, 0, 0, 0) = (\frac{m}{2}, 0, 0, 0) . \quad (48)$$

For the Feynman rule of the three-point vertex $X_2W^-W^+$, we use the following vertex which is given in [17]:

$$- \frac{i}{M_P} \left(W_{\mu\nu\ \alpha\beta}^{(W)} + W_{\nu\mu\ \alpha\beta}^{(W)} \right) , \quad (49)$$

where

$$W_{\mu\nu\ \alpha\beta}^{(W)} = \frac{1}{2} \eta_{\mu\nu} (-m_W^2 + k_1 \cdot k_2) \eta_{\alpha\beta} + k_{1\beta} k_{2\alpha} \quad (50)$$

$$+ (m_W^2 + k_1 \cdot k_2) \eta_{\mu\alpha} \eta_{\nu\beta} \quad (51)$$

$$- \eta_{\mu\alpha} k_{1\beta} k_{2\nu} - \eta_{\mu\beta} k_{1\nu} k_{2\alpha} \quad (52)$$

$$+ \eta_{\alpha\beta} k_{1\mu} k_{2\nu} . \quad (53)$$

Since $m_W^2 + k_1 \cdot k_2 = (\frac{m}{2})^2 + (\frac{m}{2})^2 = \frac{m^2}{2}$, we may write $W_{\mu\nu\ \alpha\beta}^{(W)}$ above as

$$W_{\mu\nu\ \alpha\beta}^{(W)} = \frac{1}{2} \eta_{\mu\nu} \left(-\frac{m^2}{2} \eta_{\alpha\beta} + k_{1\beta} k_{2\alpha} \right) \quad (54)$$

$$+ \frac{m^2}{2} \eta_{\mu\alpha} \eta_{\nu\beta} \quad (55)$$

$$- \eta_{\mu\alpha} k_{1\beta} k_{2\nu} - \eta_{\mu\beta} k_{1\nu} k_{2\alpha} \quad (56)$$

$$+ \eta_{\alpha\beta} k_{1\mu} k_{2\nu} . \quad (57)$$

When we work with the simplified kinematical case (48), only the second line (55) of the above expression for $W_{\mu\nu\ \alpha\beta}^{(W)}$ contributes in the present calculation.

We calculate the angular distributions of the ℓ^- and ℓ^+ for each of the possible initial gluon polarization states. We work in the X_2 rest frame, take the beam direction as the z -axis and write the gluon momenta as

$$k_1^\mu = (k_1^0, k_1^1, k_1^2, k_1^3) = (k, 0, 0, k) , \quad k_2^\mu = (k_1^0, k_1^1, k_1^2, k_1^3) = (k, 0, 0, -k) . \quad (58)$$

The polarization vectors of the initial gluons are given by (2) and (3), and we denote the polarization of the gluon which has the momentum k_1 (k_2) in (58) by ϵ_1^g (ϵ_2^g).

4.3 Angular Correlations in $gg \rightarrow X_2 \rightarrow W^-W^+ \rightarrow \ell^- \ell^+ \bar{\nu} \nu$

We consider the decays $X_2 \rightarrow W^-W^+ \rightarrow \ell^- \ell^+ \bar{\nu} \nu$ following X_2 production by gg collisions with polarizations $\epsilon_1^g = \epsilon^\pm, \epsilon_2^g = \epsilon^\pm$. Collisions with $\epsilon_1^g = \epsilon^+, \epsilon_2^g = \epsilon^+$ produce the X_2 in a $|JJ^z\rangle = |2+2\rangle$ state, whereas collisions with $\epsilon_1^g = \epsilon^-, \epsilon_2^g = \epsilon^-$ produce the X_2 in a $|JJ^z\rangle = |2-2\rangle$ state. As we saw in Section 3.2, collisions with $\epsilon_1^g = \epsilon^+, \epsilon_2^g = \epsilon^-$ and $\epsilon_1^g = \epsilon^-, \epsilon_2^g = \epsilon^+$ have vanishing amplitudes for producing the polarization state $|JJ^z\rangle = |20\rangle$ of the X_2 .

4.3.1 $|JJ^z\rangle = |2+2\rangle$

When the polarizations of the initial gluons are given by $\epsilon_1^g = \epsilon_2^g = \epsilon^+$ and the initial two-gluon polarization state is $|2+2\rangle$, the polarizations of W^- and W^+ are also given by $\epsilon_1 = \epsilon^+$ and $\epsilon_2 = \epsilon^+$. The amplitude

$$\mathcal{M} = \mathcal{M}_1 \mathcal{M}_2 = \left(\bar{u}(p_{\ell^-}) \gamma^\mu \epsilon_{1\mu} (1 - \gamma_5) v(p_{\bar{\nu}}) \right) \left(\bar{u}(p_\nu) \gamma^\mu \epsilon_{2\mu} (1 - \gamma_5) v(p_{\ell^+}) \right) , \quad (59)$$

is then, from (38) and (45), given by:

$$\frac{\mathcal{M}}{(2\sqrt{2}p)^2} = - (1 - \cos \theta_1) (1 + \cos \theta_2) e^{-i(\phi_1 + \phi_2)} , \quad (60)$$

whose absolute square is independent of the azimuthal angles $\phi_{1,2}$ and given by:

$$(1 - \cos \theta_1)^2 (1 + \cos \theta_2)^2 . \quad (61)$$

In Fig. 4(a) we plot the quantity (61) multiplied by $\sin \theta_1 \sin \theta_2$, to which $d^2\sigma/d\theta_1 d\theta_2$ is proportional.

4.3.2 $|JJ^z\rangle = |2-2\rangle$

Similarly, when the polarizations of the initial gluons are given by $\epsilon_1^g = \epsilon_2^g = \epsilon^-$ and the initial two-gluon polarization state is $|2-2\rangle$, the polarizations of W^- and W^+ are also given by $\epsilon_1 = \epsilon^-$ and $\epsilon_2 = \epsilon^-$, and from (39) and (46) the final-state lepton-antilepton angular distribution is again independent of the azimuthal angles $\phi_{1,2}$ and proportional to

$$(1 + \cos \theta_1)^2 (1 - \cos \theta_2)^2 . \quad (62)$$

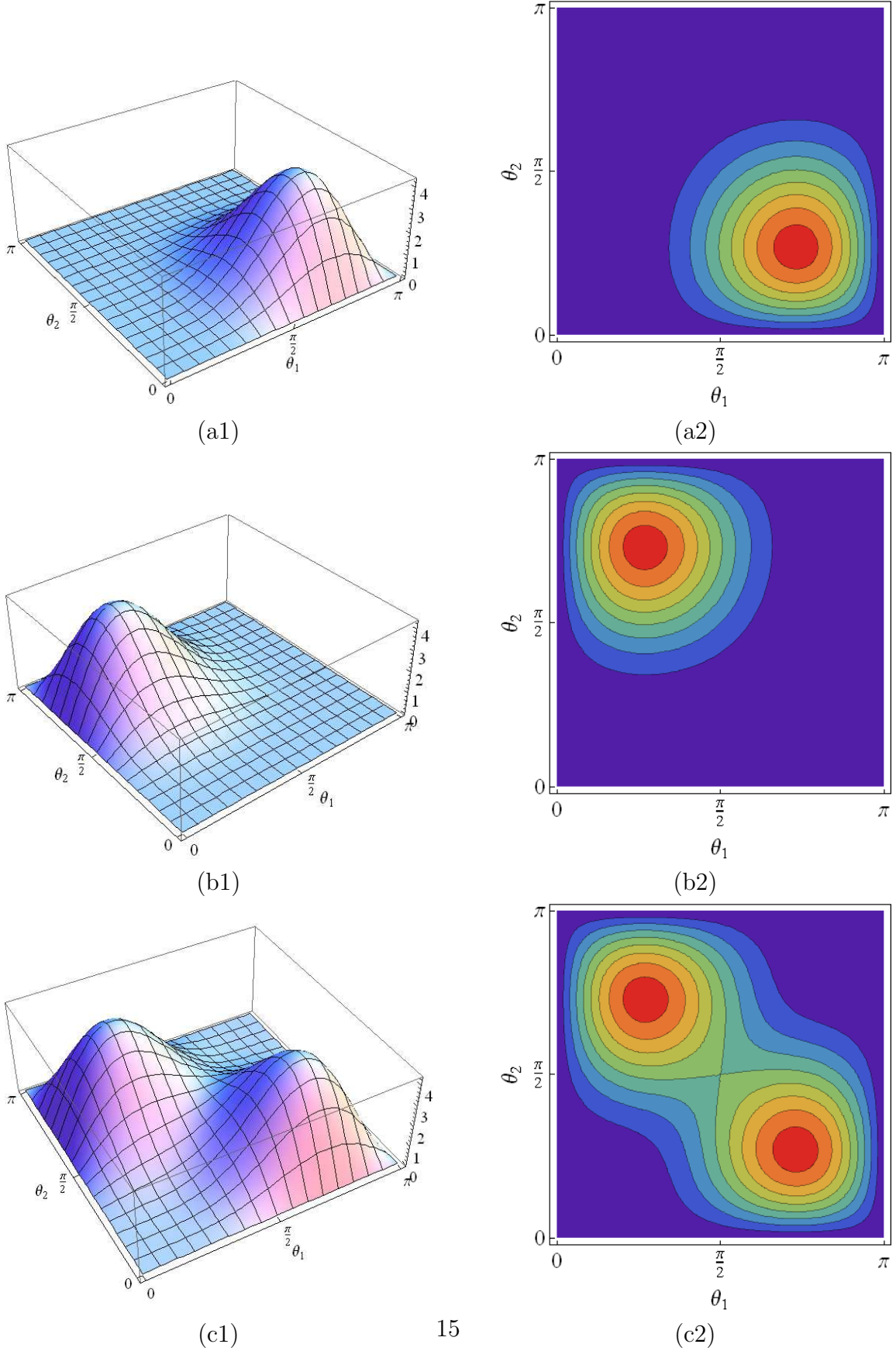


Figure 4: The angular distributions given by (a) $(61) \times \sin \theta_1 \sin \theta_2$ for decays of the $|JJ^z\rangle = |2+2\rangle$ state of $X_2 \rightarrow W^-W^+ \rightarrow \ell^-\ell^+\bar{\nu}\nu$, (b) $(62) \times \sin \theta_1 \sin \theta_2$ for decays of the $|JJ^z\rangle = |2-2\rangle$ state of $X_2 \rightarrow W^-W^+ \rightarrow \ell^-\ell^+\bar{\nu}\nu$, and (c) the sum of (a) and (b)

In Fig. 4(b) we plot the quantity (62) times $\sin \theta_1 \sin \theta_2$, to which $d^2\sigma/d\theta_1 d\theta_2$ is proportional in this case. The sum of Figs. 4(a) and (b) is plotted in Fig. 4(c).

4.4 Angular Correlations in $gg \rightarrow X_0 \rightarrow W^-W^+ \rightarrow \ell^- \ell^+ \bar{\nu} \nu$

For comparison, we now review the case of a spin-zero boson X_0 . From the Clebsch-Gordan coefficients in

$$|00\rangle = \sqrt{\frac{1}{3}}|1+1\rangle|1-1\rangle - \sqrt{\frac{1}{3}}|10\rangle|10\rangle + \sqrt{\frac{1}{3}}|1-1\rangle|1+1\rangle, \quad (63)$$

at the vertex $X_0 \rightarrow W^-W^+$ for the $|JJ^z\rangle = |00\rangle$ state of X_0 , we see that the polarizations of the W^- and W^+ are in the following coherent state:

$$\sqrt{\frac{1}{3}}\epsilon_1^+\epsilon_2^- - \sqrt{\frac{1}{3}}\epsilon_1^0\epsilon_2^0 + \sqrt{\frac{1}{3}}\epsilon_1^-\epsilon_2^+. \quad (64)$$

The state of the W^-W^+ pair produced at the $X_0 \rightarrow W^-W^+$ vertex of the spin-zero Higgs particle given by (64) is proportional to $\eta_{\alpha\beta}$.

Then, from (38, 39, 40), (45, 46, 47) and (64), we see that the amplitude \mathcal{M} of (59) is given by the following coherent amplitude (omitting a factor $1/(2\sqrt{2}p)^2$):

$$a e^{-i\phi} + b e^{i\phi} + c, \quad (65)$$

where $\phi \equiv \phi_1 - \phi_2$ and

$$a = -\sqrt{\frac{1}{3}}(1 - \cos \theta_1)(1 - \cos \theta_2) \quad (66)$$

$$b = -\sqrt{\frac{1}{3}}(1 + \cos \theta_1)(1 + \cos \theta_2) \quad (67)$$

$$c = -\sqrt{\frac{1}{3}}2 \sin \theta_1 \sin \theta_2. \quad (68)$$

The absolute square of (65) is given by

$$(a e^{-i\phi} + b e^{i\phi} + c)(a e^{i\phi} + b e^{-i\phi} + c) = a^2 + b^2 + c^2 + 2(a+b)c \cos \phi + 2ab \cos 2\phi. \quad (69)$$

In Fig. 5 we plot (69) $\times \sin \theta_1 \sin \theta_2$ (which is proportional to $d^2\sigma/d\theta_1 d\theta_2$) for $\phi = 0, \pi/2$ or $3\pi/2$, and π . The azimuthal angle distribution resulting from the integration

$$g(\phi) \equiv \int_0^\pi \sin \theta_1 d\theta_1 \int_0^\pi \sin \theta_2 d\theta_2 \left[\text{Eq. (69)} \right], \quad (70)$$

is presented in of Fig. 6.

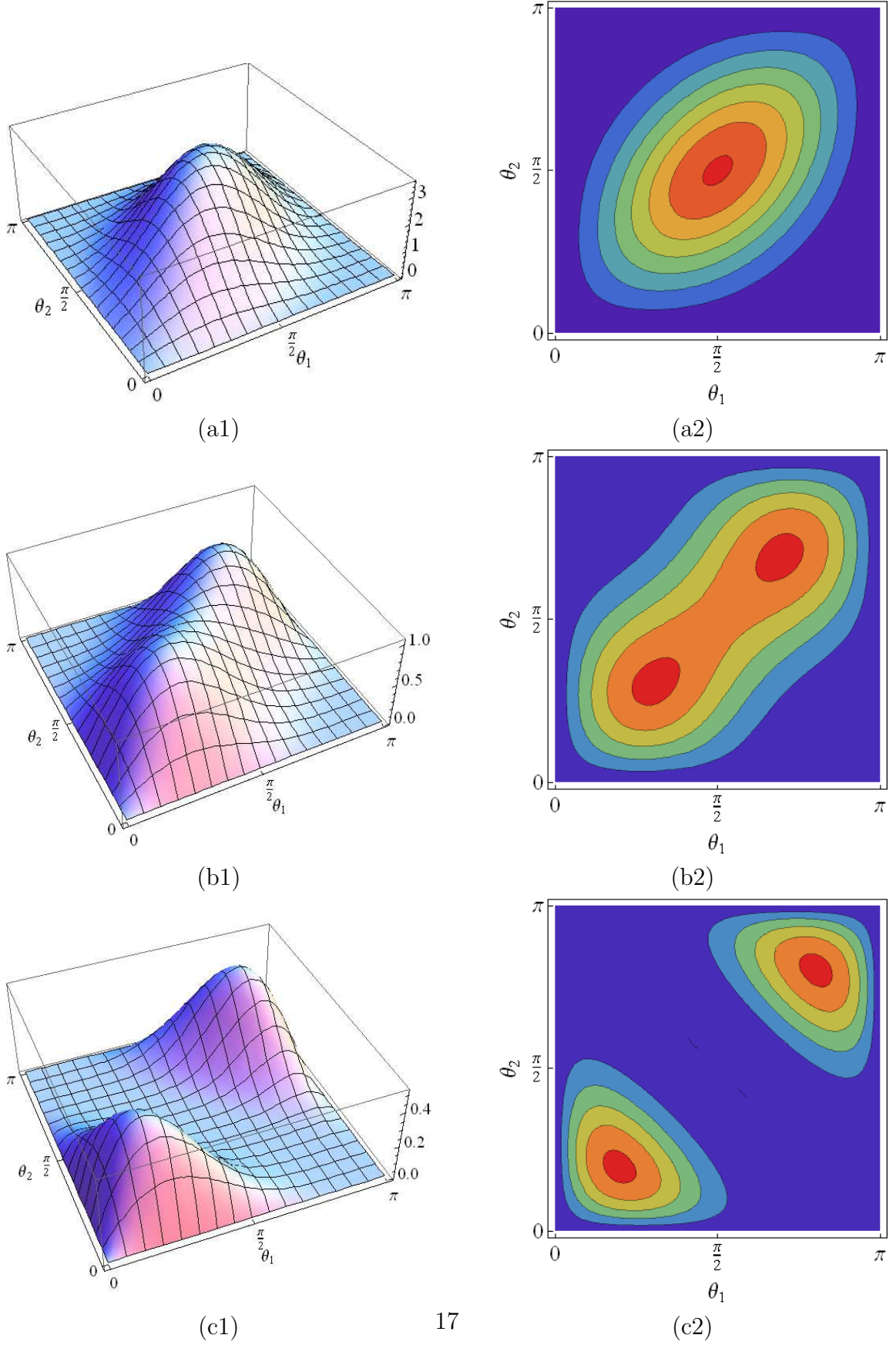


Figure 5: The angular distributions for decays of $X_0 \rightarrow W^- W^+ \rightarrow \ell^- \ell^+ \bar{\nu} \nu$ given by (69) $\times \sin \theta_1 \sin \theta_2$ for (a) $\phi = 0$, (b) $\phi = \pi/2$, and (c) $\phi = \pi$.

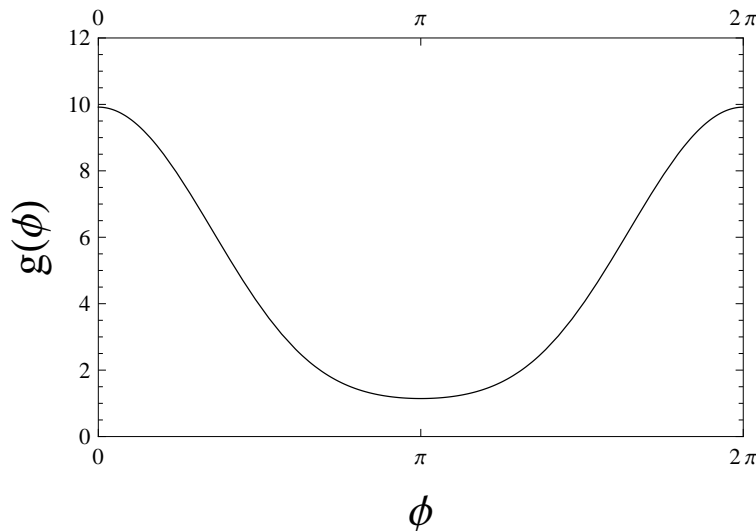


Figure 6: *The azimuthal angular distribution $g(\phi)$ given in (70) for $X_0 \rightarrow W^-W^+ \rightarrow \ell^-\ell^+\bar{\nu}\nu$ decay.*

Comparing the results presented in Fig. 6 for the X_0 case with the fact that $g(\phi)$ is constant for the X_2 case as shown in the previous subsection, we see their clear difference in the angular correlations between the ℓ^\pm . This suggests that a careful study of the ℓ^\pm angular distributions might offer some discrimination between the spin-two and spin-zero hypotheses. Moreover, the fact that the ATLAS [14] and CMS [15] W^+W^- event selections are based on the ℓ^\pm angular distributions predicted in the spin-zero case [19] might suggest that the spin-two case is already disfavoured. However, any conclusions on these possibilities would require realistic simulations of the $W^-W^+ \rightarrow \ell^-\ell^+\bar{\nu}\nu$ final states in an LHC detector.

5 Summary

We have presented in this paper analyses of the angular distributions that could be expected in the $\gamma\gamma$ and W^-W^+ decays of a hypothetical spin-two state X_2 produced at the LHC via gluon-gluon collisions, assuming that its couplings coincide with those expected for a massive Kaluza-Klein graviton. Under this hypothesis, such a spin-two particle would be produced in a definite combination of polarization states, and the polar angle distribution of the $\gamma\gamma$ final state would be predictable and non-isotropic in the X_2 rest frame, and hence distinguishable in principle from the isotropic $\gamma\gamma$ decays of a hypothetical spin-zero boson X_0 . Likewise, the angular correlations between the ℓ^\pm produced in $X_2 \rightarrow W^-W^+$ decays are predictable and distinct from those in

$X_0 \rightarrow W^-W^+$ decays. In this paper we have analyzed the case where the W^-W^+ pair is at rest, which may be a suitable first approximation to the case of a state with mass ~ 125 GeV decaying into WW^* .

This analytical study would require detailed simulations for either ATLAS and/or CMS before one could conclude whether, in practice, these angular distributions could be used to provide supplementary information about the spin of the hypothetical particle that may be responsible for the excesses of events seen at ~ 125 GeV by both ATLAS and CMS. We think that the effort of making such simulations should be worthwhile, in view of the excesses of $\gamma\gamma$ and W^-W^+ events already seen. Many other approaches to analyzing the possible spin of a Higgs candidate rely on lepton angular correlations in $ZZ \rightarrow 4\ell^\pm$ final states [2, 4, 7, 9, 10, 11, 12, 13]. These would provide considerably more information, but are limited by statistics likely to be available in the foreseeable future.

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